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AUTHORS: P. R. R. J. Stevens, H. Babinsky, F. Manar, P. Mancini, A. R. Jones, T. Nakata, N. Phillips, **R. J. Bomphey**, A. C. Gozukara, K. O. Granlund, and M. V. OI

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Experiments and Computations on the Lift of Accelerating Flat Plates at Incidence

P.R.R.J. Stevens^{*}, H. Babinsky[†]

Department of Engineering, University of Cambridge, CB2 1PZ, United Kingdom.

F. Manar[‡], P. Mancini[‡], A.R. Jones[§]

Department of Aerospace Engineering, University of Maryland, United States of America.

T. Nakata[¶], N. Phillips^{||}, R.J. Bomphrey^{**}

The Royal Veterinary College, University of London, United Kingdom.

A.C. Gozukara^{††}

MGEO Division, Aselsan Inc., Turkey.

K.O. Granlund^{‡‡}

North Carolina State University, North Carolina, United States of America.

M.V. Ol^{xo}

U.S. Air Force Research Laboratory, Wright-Patterson AFB, Ohio, United States of America.

This paper discusses the force history and flow topology of accelerating flat plate wings. The work is a collaborative effort to study fundamental, unsteady low Reynolds number flows. The motion kinematics are designed to be relevant to the Micro-Air Vehicle flight regime. A combination of experimental and computational techniques are used to obtain data for comparison. There is a striking correlation of lift history data and flow topology from both experimental and computational datasets. It is found that the Leading / Trailing Edge Vortex core separation during the initial part of a surge motion can be reasonably well approximated by $c \cdot \cos \alpha$ and the Leading / Trailing Edge Vortex relative advection velocity is estimated to be $0.5 \cdot U_\infty$. This Leading / Trailing Edge Vortex relative advection velocity is a useful measure of how quickly the Trailing Edge Vortex moves away from the Leading Edge Vortex, which can influence lift for accelerating flat plates at high incidence angles.

Nomenclature

a	Non-dimensional distance over which wing accelerates
a_s	'Eldredge' transition smoothing parameter
c	Wing chord, m
$c_{l,circ}$	2D, circulatory lift coefficient
R	Resolution of LEV trajectory measurement, [Hz]
s	Distance of wing travel, [m]
s/c	Non-dimensional distance travelled in chord lengths
t	Time, [s]
t_1	Time at the start of surge, [s]
t_2	Time at the end of surge, [s]
u	Velocity in x-direction, [ms^{-1}]
u_{LEV}	LEV advection velocity, [ms^{-1}]
u_{TEV}	TEV advection velocity, [ms^{-1}]
U_∞	Reference velocity, [ms^{-1}]
x_{LEV}	x -position of LEV relative to LE of wing
x_{TEV}	x -position of TEV relative to TE of wing
α	Angle of incidence, [$^\circ$]
α_0	Maximum angle of incidence, [$^\circ$]
Γ	Circulation, [m^2s^{-1}]
Γ_{LEV}	LEV Circulation, [m^2s^{-1}]
Γ_∞	Theoretical steady state circulation assuming attached flow, [m^2s^{-1}]
\mathcal{R}	Aspect Ratio
LE	Leading Edge

*Research Associate, Cambridge University Engineering Department Aerodynamics Lab, Member AIAA, robbie.stevens@cantab.net

[†]Professor of Aerodynamics, Cambridge University Engineering Department Aerodynamics Lab, Associate Fellow AIAA, hb@eng.cam.ac.uk

[‡]Department of Engineering, University of Maryland, College Park, AIAA Student Member.

[§]Assistant Professor, Department of Engineering, University of Maryland, College Park, Associate Fellow AIAA.

[¶]Project Assistant Professor, Graduate School of Engineering, Chiba University, Japan.

^{||}Research Associate, Department of Comparative Biomedical Sciences, Royal Veterinary College, University of London.

^{**}Reader, Department of Comparative Biomedical Sciences, Royal Veterinary College, University of London.

^{††}Senior Engineer, MGEO Division, Aselsan Inc.

^{‡‡}Assistant Professor, Department of Mechanical and Aerospace Engineering, Raleigh, AIAA Senior Member

^{ˆˆ}Technical Advisor, Aero Configurations Branch, Aerospace Systems Directorate, Associate Fellow AIAA.

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2	<i>LEV</i>	Leading Edge Vortex
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4	<i>LIC</i>	Line Integral Convolution
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6	<i>TE</i>	Trailing Edge
7		
8	<i>TEV</i>	Trailing Edge Vortex
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11 I. Introduction

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14 The unsteady lift generation of flapping wings is of interest for Micro-Air Vehicle
15 (MAV) design and additionally to better understand natural fliers. A MAV is a small
16 aerial vehicle which has classically been described as having a wingspan of 15cm or
17 less [1]. The MAV scale corresponds to the size and flight speed of small birds and larger
18 insects and produces Reynolds numbers in the range of 10^4 - 10^5 [2].
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21 The mechanism of how flapping wings generate large stroke averaged lift coefficients
22 (see for example Lentink and Dickinson [3]) was the motivation for NATO task group,
23 AVT-149 [4]. The AVT-149 work lead to insight into how lift is connected to wing geometry,
24 flapping kinematics and Reynolds number etc. To gain a better understanding of unsteady
25 lift generation mechanisms, one approach is to investigate simplified but well controlled
26 canonical cases. Dickinson and Götz [5] investigated the unsteady forces and flowfield
27 for a wing translated in a stationary fluid for Reynolds numbers of $O10^3$ and studied the
28 Wagner effect and Dynamic Stall. Later Beckwith and Babinsky [6] conducted similar
29 work but with a finite wing, finding that accelerating wings at high incidence can produce
30 high lift coefficients. Ringuette et al. [7] performed experiments on *impulsively started*
31 flat plates normal to the motion direction. Interestingly they described the drag force on
32 the plate according to Batchelor's [8] formulation which depends on an impulse which is
33 dependent upon the circulation of the LEV pair created.
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Chen et al. [9] performed a computational study on a flat plate at high incidences at
low Reynolds numbers (in the range of 10 - 200) with accelerations governed by a power
law and found that the computed lift revealed an LEV-induced lift augmentation evident
across all powers and angles of attack. Baik et al. [10] studied both pitching and plunging
aerofoils for Reynolds numbers in the range 5000 - 20,000 and interestingly found that the
Reynolds number has a small effect on aerodynamic force generation.

Despite the very informative studies conducted by other researchers, it is clear that
there is a need for a more detailed investigation the force contributions for accelerating
flat plate wings at high incidences. Past studies have also demonstrated the usefulness
of comparisons between numerical and experimental results for similar kinematics and
Reynolds numbers (see for example Bansmer and Radespiel [11] who investigated an
aerofoil undergoing an acceleration in the direction of the freestream velocity at a Reynolds

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Number of 100,000).

The work described in this paper is the result of studies undertaken as part of the NATO RTO task group AVT-202, '*Advances in Fundamental Unsteady Low Reynolds Number Flows*' [12]. This paper focusses on one particular aspect of the work, namely the insight gained from one of the canonical test cases defined by the task group. A typical flowfield for one of these simplified flapping motions features flow separation at the leading edge, a Leading Edge Vortex (LEV) and a starting or Trailing Edge Vortex (TEV). This observation inspired companion work within the AVT-202 task group on a simple low-order model [13], where the force is broken down into vortex lift and a non-circulatory, '*virtual mass*' (inertial) force^a. The vortex lift is assumed to be caused by a LEV/TEV pair. The work contained herein forms the foundation for the companion work on the task group's low-order lift force model. The canonical surging wing case motion kinematics are outlined and the results are presented in terms of the aerodynamic forces, the flow topology and the strength and position of the Leading and Trailing Edge Vortices (LEV and TEV). Finally, we present a brief explanation of how the data contained herein contributes to the companion work on the aforementioned low-order model.

A. Motion Kinematics

All the case data discussed in this paper involve a flat plate wing with a rounded Leading Edge (LE), surging^b over a streamwise distance of either 1 chord (1c, fast case) or 6 chords (6c, slow case). The wing (of Aspect Ratio (R) 4 for the canonical case) is accelerated (over 1c or 6c) at a constant incidence of 45° to a Reynolds number of 20,000 (canonical case) and continues to translate at a constant velocity thereafter. The canonical case is designed to be simplistically representative of MAV flight regime style kinematics. Figure 1 shows a breakdown of the motions that make up typical flapping stroke on a flying insect. The work described here focusses exclusively on the simple linear translation in the hope of gaining a greater appreciation of the underlying fundamental physics of flapping flight.

Variations of the wing Aspect Ratio (R) and Reynolds number are highlighted where appropriate. The kinematics are represented simplistically in Figure 2.

Both the fast acceleration over 1c and slow acceleration over 6c cases have a constant acceleration, which produces a theoretical velocity variation, which is quadratic in space as shown in Figure 3. They show the non-dimensional velocity, u/U_∞ plotted against '*advective time*', s/c . The velocity is non-dimensionalised by the steady state freestream velocity. Advective time is the distance travelled by the wing, s non-dimensionalised by the wing chord, c . While under acceleration, the surge velocity profile is described by the

^a'Virtual' or 'Added' mass is an inertial reaction force which contributes to lift when a wing is accelerated in a fluid from rest and a mass of fluid is accelerated with the wing.

^b'Surging' here refers to a constant acceleration from rest to a steady state velocity in a quiescent fluid.

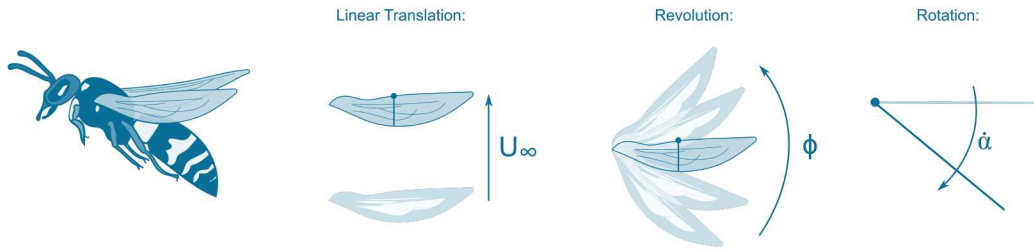


Figure 1: Simplification of flapping wing kinematics into a linear translation, revolution and rotation. Linear translation is the motion of interest in this work.

following expression:

$$\frac{u}{U_\infty} = \frac{U_\infty t}{2ac} \quad \text{for } t < t_2 \quad \text{and} \quad \frac{u}{U_\infty} = 1 \quad \text{for } t > t_2 \quad (1)$$

where t is time and a is a non-dimensional distance over which the wing accelerates. U_∞ is the velocity which corresponds to the steady state freestream condition, whereas u represents the instantaneous velocity so under steady state conditions this becomes $u = U_\infty$. The surge velocity profile may be described in terms of advective time by the following modified form of the above expression:

$$\frac{u}{U_\infty} = \sqrt{\frac{1}{a}} \cdot \sqrt{\frac{s}{c}} \quad \text{for } s/c < a \quad \text{and} \quad \frac{u}{U_\infty} = 1 \quad \text{for } s/c > a \quad (2)$$

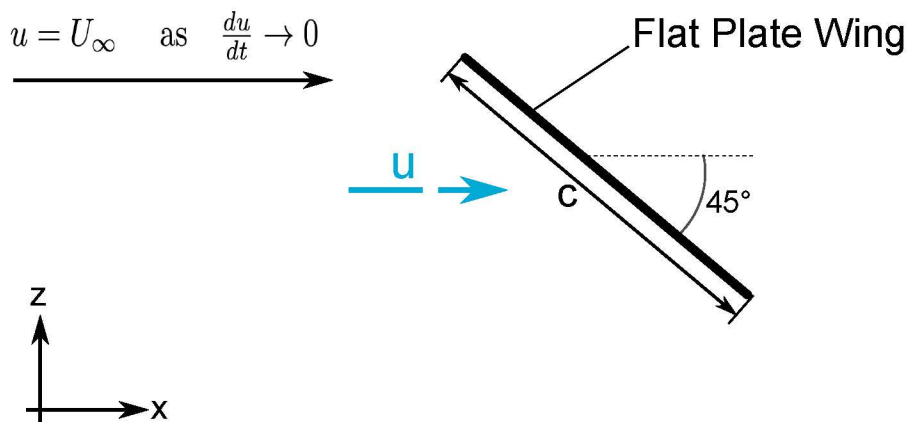


Figure 2: Canonical flat-plate wing surge kinematics.

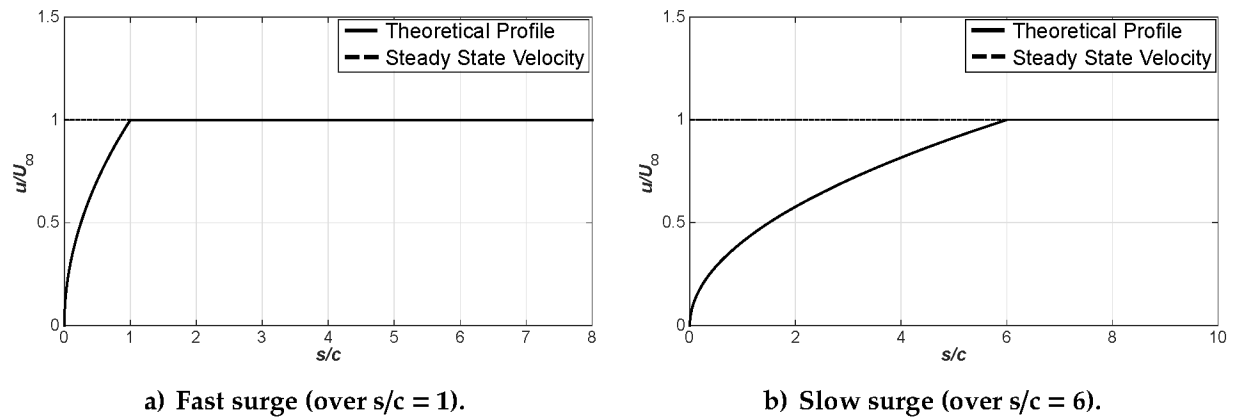


Figure 3: Surge velocity profiles, steady state $Re = 20,000$.

B. Link to Low-Order Model

A key aspect of this paper is how experimental and computational data can be used to inform the development of a low-order model of the lift force [13]. It is identified there that the force may be separated into circulatory (viscous) and non-circulatory (inertial) contributions. The non-circulatory contribution is determined theoretically. It is shown however that the determination of circulatory lift requires knowledge of Leading Edge Vortex (LEV) and Trailing Edge Vortex (TEV) positions and velocities relative to the plate, and the circulation of the LEV according to the following expression:

$$c_{l,circ} = -\frac{2}{U_{\infty}^2 c} \left[(u_{LEV} - u_{TEV})\Gamma_{LEV} + (x_{LEV} - x_{TEV})\dot{\Gamma}_{LEV} \right] \quad (3)$$

The values that need to be informed through experimental data may therefore be summarised as follows:

1. A LEV/TEV core separation distance, $(x_{LEV} - x_{TEV})$.
2. A LEV/TEV, relative advection velocity, $(u_{LEV} - u_{TEV})$.
3. The circulation of the LEV, (Γ_{LEV}) and the rate of growth of LEV circulation $(\dot{\Gamma}_{LEV})$.

The major assumption in attempting to determine the above values is that a distinct LEV and TEV form, which have equal but opposite strengths. Further, it is assumed that all the circulation which contributes to the lift may be considered to be that associated with the LEV and that bound circulation is negligible. In reality of course not all the circulation will necessarily be contained within the LEV but the implications of these assumptions seem to be small and are discussed in detail by Babinsky et al. [13]).

Figure 4 shows an adapted version of the comparison of force data alongside the prediction made by the low-order model of Babinsky et al. [13]. The authors state that the

work did not aim to accurately predict lift but rather to identify various circulatory vs. non-circulatory forces, helping the understanding of the connection between unsteady force production and kinematics.

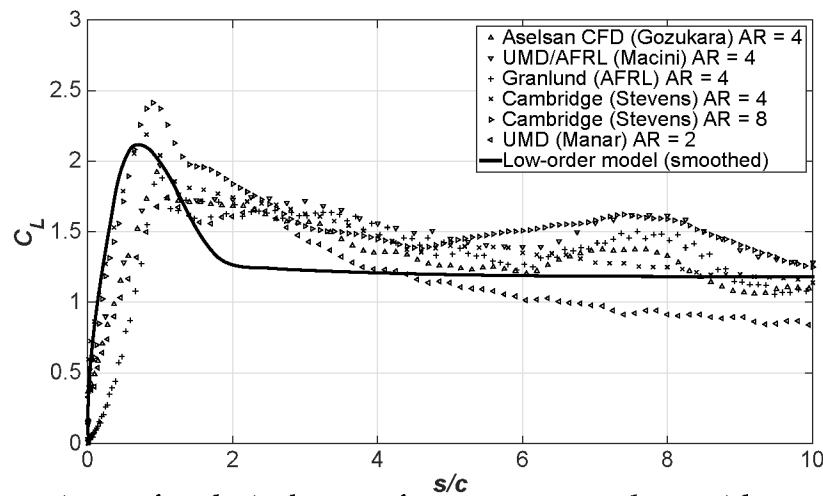


Figure 4: Comparison of technical team fast surge case data with surging theoretical model. Adapted from the companion work of Babinsky et al. [13].

The motivation of this paper is twofold: first to compare lift histories and flow topologies across a range of facilities and computational approaches and secondly to provide estimates of the aforementioned LEV and TEV parameters that are used in the prediction of the circulatory lift force in the companion work 'Low Order Modelling of Lift Forces for Unsteady Pitching and Surging Wings' [13].

II. Methods

This section overviews the facilities and methods used by the respective groups to obtain data. Data comes from two different experimental arrangements and two different computational approaches, giving a total of four independent data sources.

A. Experiments

1. University of Cambridge

The Cambridge University Engineering Department (P.R.R.J. Stevens and H. Babinsky) water towing tank facility is used for experiments. A schematic of the tow tank facility is shown in Figure 5. Experiments are conducted in water to take advantage of Reynolds scale effects. The tank has a 2m long working section with clear side walls and floor for laser and camera optical access. The operational cross-section is 0.8m^2 . A physical $\mathcal{R} = 2$ wing is used, which coupled with a surface skim plate to act as a symmetry plane, gives an effective \mathcal{R} of 4. The wing has a chord length of 0.12m and a thickness of 2.5%. For

the physical $R = 2$ wing, blockage (at $\alpha = 45^\circ$) is 2.5%. Experiments are conducted at Reynolds numbers of 10,000 and 20,000.

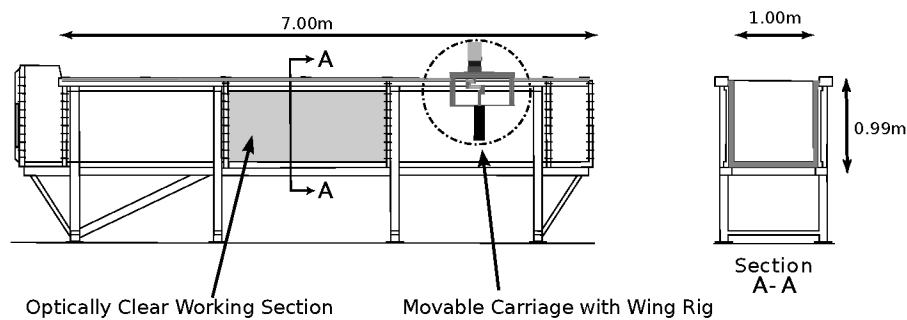


Figure 5: Tow tank facility schematic. (Adapted from Morgan [14])

There is a movable carriage mounted on top of the tank for towing the wing. The computer-controlled carriage can achieve a positional accuracy of $\pm 0.25\%$. The acceleration ramp is smoothed using an Eldredge smoothing function (see Section II.B.1 for details). The carriage velocity is corrected for temperature variations greater than 1°C , giving a maximum error in freestream Reynolds number of 1.25%.

Lift forces are measured with a *Flow Dynamics* force balance of the strain gauge, load cell type. The two component balance has a range of $\pm 50\text{N}$ and an accuracy within 0.01N. The balance is calibrated using known masses. Data is acquired at 1kHz and averaged over 10 runs. The data is smoothed using a moving-point average span of 100 data points with the endpoints treated by having progressively smaller span widths. To extract the pure fluid mechanical forces, it is necessary to subtract the inertial forces on the wing. This is done by performing the motion kinematics in air and assuming that the data acquired is representative of the inertial force exerted. This is valid if it is assumed that the aerodynamic forces in air are assumed small with respect to the inertial.

2. U.S. Air Force Research Lab

Data was taken in the United States Air Force Research Lab, Aerospace Systems Directorate's water tunnel, by K.O. Granlund and M.V. OL and separately by P. Mancini and A. Jones, thus producing two data sets. The tunnel is of the free-surface type, with test section 18" wide, 24" high and 96" long. The tunnel is fitted with a three degree of freedom motion system, consisting of three linear electric servomotors and a programmable controller. Two motors vertically oriented above the test section can be used to actuate pitch and plunge motions, while the third motor is used for the surge motions discussed in this paper. The surge motion is conducted, with the tunnel shut off and the two vertical motors set to place the model at 45° incidence. Experiments are conducted at $\text{Re} = 20,000$.

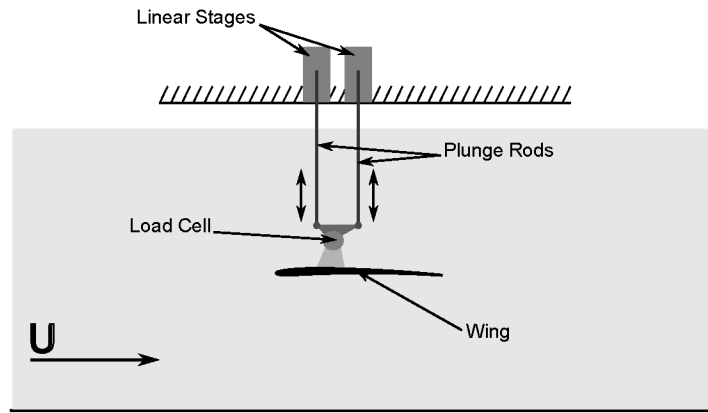


Figure 6: United States Air Force Research Lab, Aerospace Systems Directorate's water tunnel configuration.

The $R = 4$ carbon fibre plate with $c = 0.0762\text{m}$ and thickness $\sim 4\%$ model is mounted horizontally in the test section, with a central support also housing the *ATI Nano-25* 6-component force balance, which has a limiting range of $\pm 125\text{N}$ and an accuracy of 0.02N . The plate is mounted offset from the load cell by a $2.25''$ 3D-printed plastic strut. Flow visualisation is conducted at $1c$ outboard from the wing's mid-span location.

Processing/filtering of force-data is discussed by Granlund et al. [15] with low-pass filtering ultimately limited by the system natural frequency, typically at $\sim 13\text{Hz}$ in post-processing, and at 18Hz in the load-cell's native acquisition system, with sampling at 1KHz . The system natural frequency was determined by a strike-test of the model.

B. Computations

1. Royal Veterinary College

CFD analysis is performed by the Royal Veterinary College (RVC) group (T. Nakata, N. Phillips and R.J. Bomphrey) with a versatile CFD-based dynamic flight simulator [16] that is based on three-dimensional, incompressible and unsteady Navier-Stokes equations. The wing is modelled by a single block ($101 \times 101 \times 101$) that has a non-dimensional chord of 1 and uniform thickness of 1% with elliptical smoothing at all edges. The distance from the wing surface to the outer boundary is set to $18c$. Translational velocity profiles were computed using the 'Eldredge function' [17], which is a method to smooth a surge profile. After Eldredge [18], the wing incidence, $\alpha(t)$ is described by the following function:

$$\alpha(t) = \alpha_0 \frac{G(t)}{G_{max}} \quad (4)$$

where,

$$G(t) = \log \left[\frac{\cosh(a_s U_\infty (t - t_1)/c)}{\cosh(a_s U_\infty (t_1 - t_2)/c)} \right] - a_s U_\infty (t_1 - t_2)/c \quad (5)$$

$$G_{max} = 2a_s U_\infty (t_2 - t_1)/c \quad (6)$$

where, α_0 is the maximum angle, t_1 is the time at the start of surge and t_2 is the time at the end of surge. The profiles were designed to reach constant velocity after 6 chords of travel. The RVC computations were performed using the prescribed canonical case geometry but with the Reynolds number set to 660.

2. Aselsan

The Aselsan group (A.C. Gozukara) computed the fast surge case at a chord based Reynolds number of 10,000 using ANSYS Fluent 15.0. The computation was performed with an unstructured moving mesh composed of two zones; an outer grid surrounding an inner one, moving with the plate without going through a deformation. The outer zone is morphed and regenerated according to the predefined deformation rules to enable the inner zone to move. Mid-span cross-section grid slices are shown in Figure 7. The grid for RANS computations has 19426144 tetrahedral elements. Slightly smaller grids are used for laminar computations. The domain is $80c$ long, $40c$ wide and $40c$ high. The plate has a chord of 60mm , thickness of $\sim 3.3\%$, and $\mathcal{R} = 4$. The computation is run as RANS with a $k-\epsilon$ turbulence model. One chord of travel is divided into 500 equal time steps. A $\text{Re} = 3600$ case has also been computed with flow solutions obtained by solving unsteady, laminar flow equations.

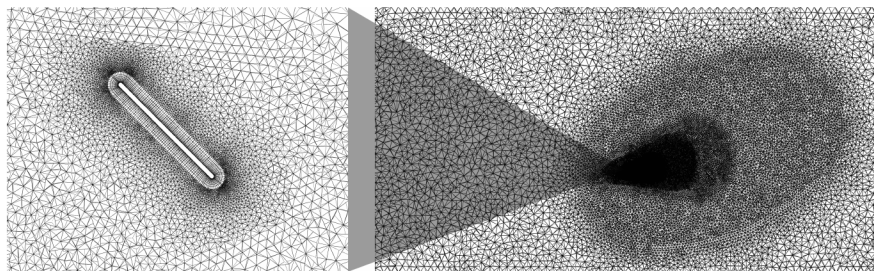


Figure 7: Cross-sectional view of Aselsan group's (A.C. Gozukara) unstructured grid.

C. Discrepancies in Approach

All groups are using a rectangular planform, $\mathcal{R} = 4$ wing for the canonical case, with a rounded LE and TE shape. Despite this effort to remain consistent, there are differences in the precise rounding of the LE and TE between all groups. It is also noted that the

1
2 boundary conditions for experiments differ from each other as well. The Cambridge
3 group uses a physical $R=2$ wing and a skim plate acting as an image plane, whereas
4 the United States Air Force Research Lab uses a sting mounted wing with a physical $R=$
5 4 wing. The difference in experimental boundary conditions could therefore have some
6 effect on the flows experienced. For the Cambridge setup, there may be some influence of
7 the the gap between the wing and the skim plate, so to mitigate this, the gap is set at 1mm
8 after the recommendation of Son et al. [19] who suggest that if a symmetry plane is used,
9 the gap should be less than 2mm. For the United States Air Force Research Laboratory
10 setup, the plastic strut will influence the flow in the central region of the wing. In practice
11 however, it is found that generally such effects are small or difficult to discern. There are
12 also some variations in the Reynolds number between cases, but it will be shown that there
13 seems to be Reynolds number independence across the datasets. It is also recognised that
14 despite all efforts to adhere closely to the acceleration velocity profile, across the methods,
15 small differences in the transition region between the surge motion and constant velocity
16 motion thereafter may affect force measurements but again it will be shown that the effect
17 is relatively small.
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29 III. Results

30 The canonical case is first discussed in terms of force history and flow topology. This
31 allows a general appreciation of how specific flow features correlate to the forces at given
32 instances. In the companion paper on the low-order model of the lift force, the LEV and
33 TEV trajectories extracted from the data here are used to give position information and
34 an approximation of their relative advection velocity.
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40 A. Force History

41 Figure 8 compares lift coefficient histories for the fast and slow surge cases respectively.
42 The lift is plotted against an advective timescale, s/c .^c It is immediately recognised that
43 there is good agreement between different datasets. Considering the fast case of Figure 8 a,
44 at first, there is an initial spike in lift, followed by a drop. The same trends are captured
45 by all datasets astonishingly well, namely, the initial peak in lift, followed by a short,
46 sharp drop, then a slow decay in lift before (with the exception of the data of Stevens) a
47 second maximum in lift and finally an asymptotic decay to a steady state lift coefficient.
48 Consider Figure 8c, which shows a zoom of the early portion of the lift history. The peak
49 lift coefficient occurs towards the end of the first chord of travel within 15% of $s/c = 1$ for
50 all cases. The rates of growth, up to the first lift maximum are also quite similar in trend,
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57 ^cThe advective time s/c as used here, corresponds to the non-dimensional distance travelled.
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2 with the data having an approximately linear increase.

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4 There are some subtle differences in how the lift increases up to the first maximum,
5 with the data of Stevens showing a higher lift while surging and a peak lift that is 10%
6 greater than any other, whereas the data of Granlund has a peak lift that is 17% lower than
7 any other. There is also a very noticeable difference in the initial value of lift at $s/c = 0$ for
8 all cases, which varies from $c_l \approx 0.2$ (Mancini) to $c_l \approx 0.6$ (Stevens). Some of the differences
9 which are observed may be accounted for by the type of data filtering and smoothing
10 applied by each group. Returning to Figure 8 a, after the first maximum, there is initially
11 a small but nonetheless, sharp drop in lift, this is followed by a slow decay which persists
12 until approximately $s/c = 6$. The datasets of Gozukara, Mancini and Granlund then all
13 show a similar second maximum in lift around $s/c = 7.5$. Interestingly, this feature is
14 apparent in the data of Stevens, although there is a smaller, less distinct second maximum
15 a little earlier at around $s/c = 6$. The data of Stevens however shows that it takes long
16 advective timescales for a steady state condition to be approached (around $20s/c$ in this
17 case).
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21 The experimental datasets generally show good agreement with the single CFD dataset
22 of Gozukara, giving confidence in both the accuracy of the experimental datasets and
23 the quality of the CFD. A typical deviation from the mean at $s/c = 5$ for example is
24 approximately $\pm 10\%$.
25

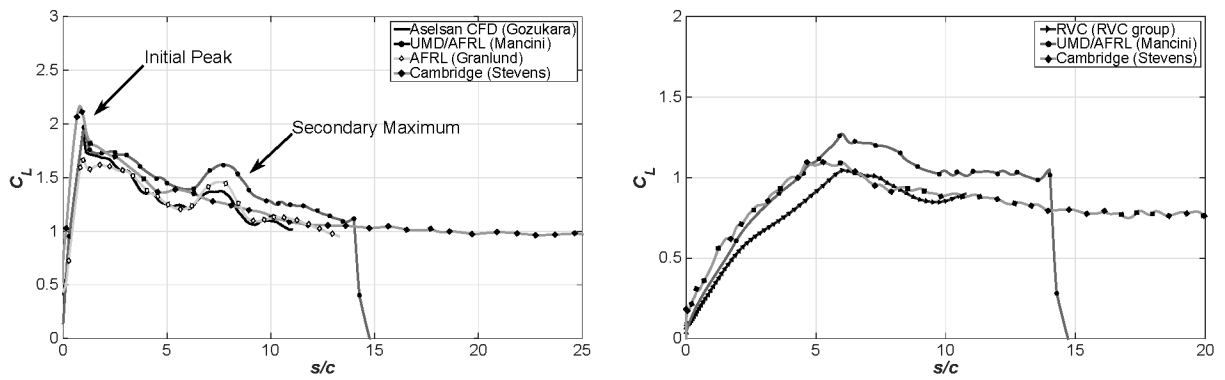
26
27 The slow surge lift history of Figure 8 b shows a rise in lift, peaking at approximately
28 $s/c = 6$. There is an absence of a secondary rise in forces. The lift trace of Stevens shows a
29 flattening of the lift coefficient around $s/c = 15$. The value of the asymptotic lift coefficient
30 here is approximately 25% of that observed where the curve flattens in the fast surge case,
31 suggesting that this is not yet the true steady state lift coefficient. It may be that a much
32 longer advective timescale is required to study this phenomenon.
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41 **B. Flow Topology**

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43 The discussion in this section is qualitative, with a quantitative investigation of the vortex
44 dynamics and strength to follow in subsequent sections.
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47 Figures 9 and 10 show the comparison of flow visualisation with vorticity fields with
48 vectors superimposed from PIV and CFD data for the fast surge case. All figure dimensions
49 are non-dimensionalised by the wing chord, c , clockwise fluid rotation is coloured blue
50 with anti-clockwise rotation coloured red.
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52
53 The data of Figure 9 are arranged to show the comparison of the initial development
54 of the flow and the formation of the LEV, followed by the breakup of the LEV. There is
55 no TEV structure present within the limited field of view for PIV data but this is clearly
56 visible in the flow visualisation and CFD data for $s/c = 0.5$ and 1.5 . A distinct LEV structure
57 has already formed at $s/c = 0.5$. In the PIV data, a shear layer emanating from the TE is also
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a) Fast surge lift coefficient history.

b) Slow surge lift coefficient history.

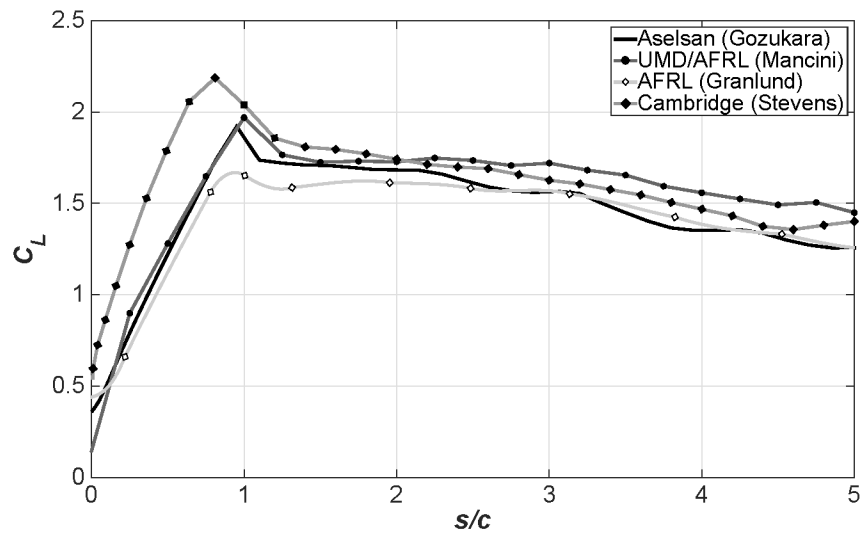
c) Zoom of lift history for early s/c for the fast surge case..

Figure 8: Lift coefficient histories for fast and slow surge cases respectively.

visible, even though the TEV is not. By $s/c = 1.5$, the LEV core has grown and advected aft of the LE of the wing in x , with hardly any change in the y -position. Additionally it is noted that the LEV has moved downstream from the LE less than the $s/c = 1$ movement of the plate and hence is considered still somewhat 'attached'. At $s/c = 2.5$, the LEV core has advected further aft, with a noticeable dispersion of the LEV beginning to occur. The TEV seen initially is still visible in the flow visualisation but in the CFD data it has now advected out of the field of view. Closer inspection of the flowfields indicates some variance in the LEV core position between the respective techniques although the general topology is remarkably similar.

Figure 10 shows the flow development for $s/c \geq 3.0$. The PIV shows a marked loss of LEV coherency by $s/c = 3.0$, which is in contrast to the flow visualisation and CFD, where the LEV is still reasonably well defined. For all three methods, the flow appears stalled at

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2 $s/c = 5.0$, although there is some new recirculating flow close to the LE, this is not coherent
3 like the LEV previously observed. At $s/c = 8.0$, there is no flow visualisation available but
4 comparison of the PIV and CFD shows that a body of slowly recirculating fluid has formed
5 above the wing, which is unusual and may be a streamline pseudo-reattachment of the
6 flow. This pseudo-reattachment likely explains the presence of the second lift maximum,
7 which was noticed to occur around $s/c = 7.5$.

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11 Figure 11 compares flow visualisation and PIV data ($Re = 20,000$) in the first and second
12 columns respectively with CFD data ($Re = 660$) in the third and fourth columns for the
13 slow surge case. Once more, all dimensions are non-dimensionalised by the wing chord,
14 c . Data is again presented with clockwise fluid rotation coloured blue with anti-clockwise
15 rotation coloured red. The CFD in the third column shows vorticity with velocity vectors
16 superimposed for a direct comparison with PIV data. In addition Figure 11 also shows
17 images generated using the Line Integral Convolution (LIC) technique [20] to visualise
18 the CFD data.

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24 Initial cross-examination of the flow visualisation, PIV and CFD data suggests that
25 there is some agreement in the general nature of the flow structures observed.

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28 Turning in detail to the flow visualisation in the left hand column of Figure 11, there
29 is initially at $s/c = 1.5$, a LEV structure visible and this is also reflected in the PIV and CFD
30 data. By $s/c = 3$, there is an absence of a clear LEV structure. Upon closer inspection of the
31 vector field, there is a clockwise rotational tendency above the wing, however the vorticity
32 colouring suggests that this rotation is weak. The CFD data does however seem to show a
33 more distinct LEV. A direct comparison of the PIV flowfields may be made with the CFD
34 flowfields of the third column. The CFD vectors show more distinct vortical structures
35 and these are made very apparent by the LIC processing in the right hand column. In
36 contrast, the flow visualisation and PIV data suggests that such structures are weak if they
37 exist at all and the flow is more akin to separation. There may be some Reynolds number
38 effect here but this is not strongly reflected in the force history.

44 45 **C. LEV and TEV Position**

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47 The previous analysis of the flow topology has shown that LEV structures are particularly
48 noticeable in the fast surge case, where they slowly advect away from the wing as it
49 continues to move in translation. Here, vortex trajectories are tracked relative to the LE for
50 the LEV and Trailing Edge (TE) for the TEV respectively^d. The position of the individual
51 LEV and TEV in space enables their core separation, $(x_{LEV} - x_{TEV})$ to be estimated and
52 this in turn allows their relative advection velocity $(u_{LEV} - u_{TEV})$ to be determined. These

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57 ^dFlowfields with the TEV visible are not shown in this paper but positional data was extracted from PIV
58 datasets.

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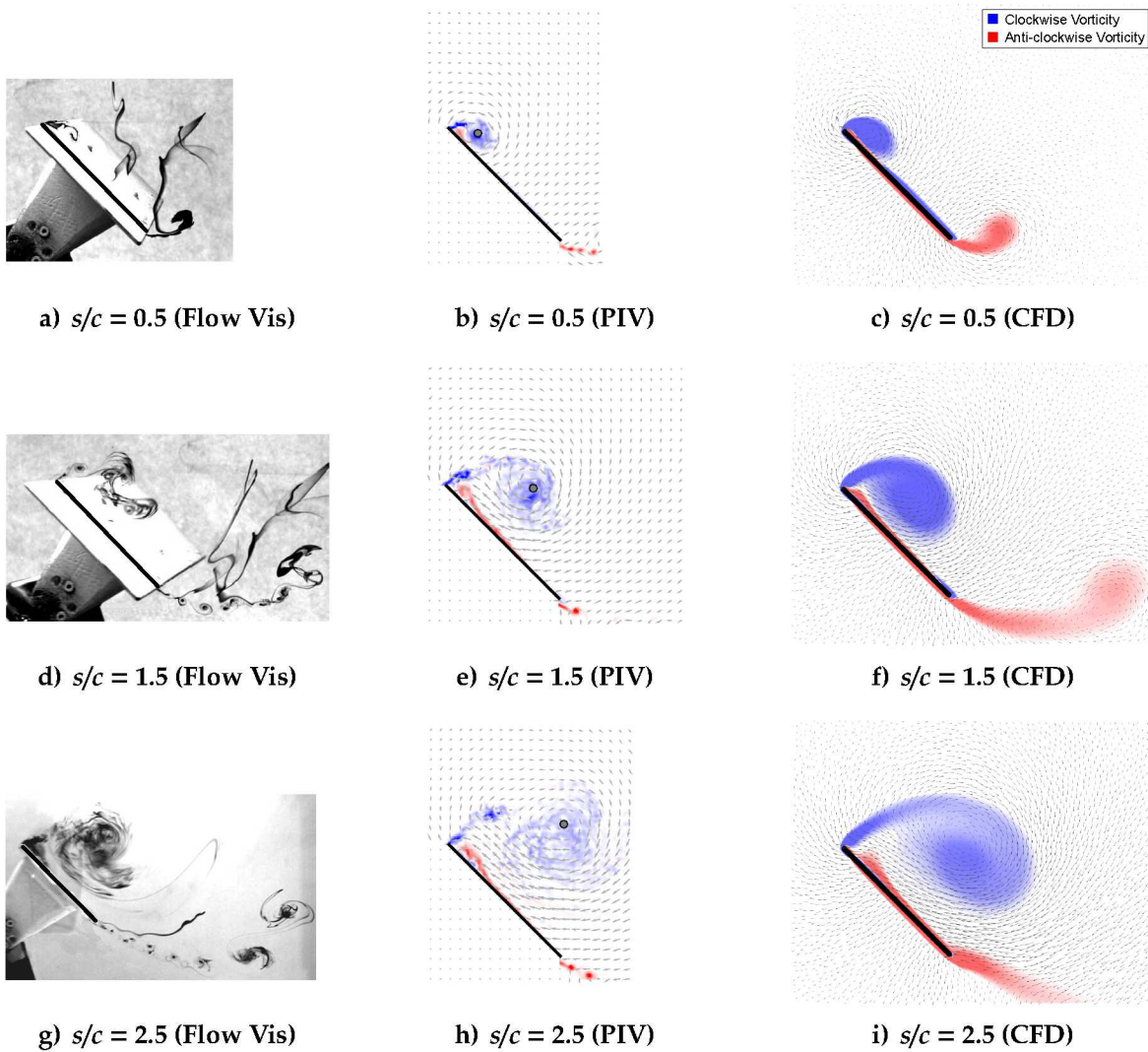


Figure 9: Comparison of fast surge flow fields from AFRL dye flow visualisation in the left hand column, UMD/AFRL PIV data showing vorticity field with vectors superimposed in the middle column and Aselsan CFD vorticity field with vectors superimposed in the right hand column for early advective times.

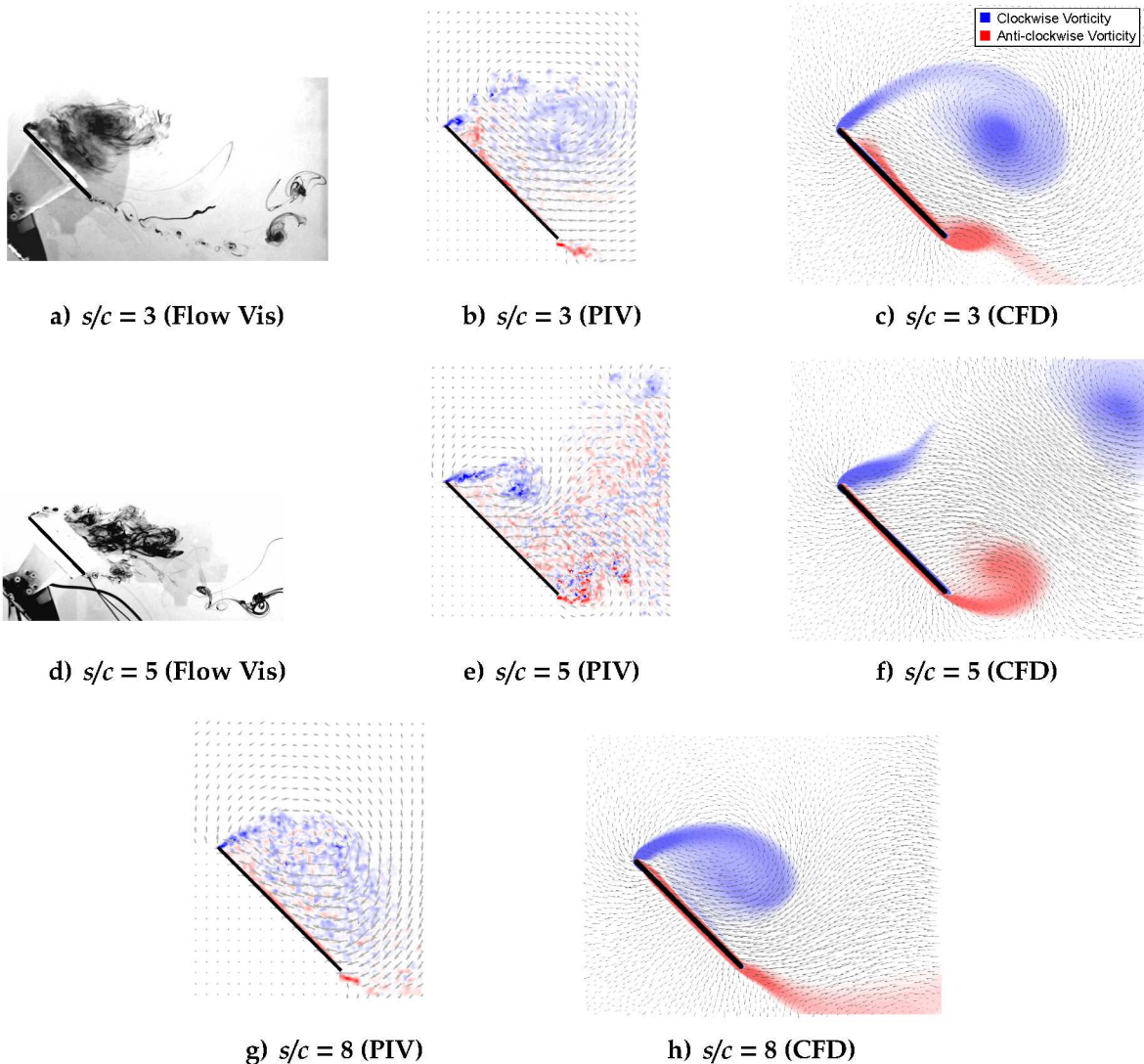


Figure 10: Comparison of fast surge flow fields from AFRL dye flow visualisation in the left hand column, UMD/AFRL PIV data showing vorticity field with vectors superimposed in the middle column and Aselsan CFD vorticity field with vectors superimposed in the right hand column for later advective times.